

$$\#1: \left(x - \frac{1}{4}\right)^{1/2} \cdot \left(y - \frac{1}{4}\right)^{1/2}$$

A) Marginal productivities:

$$\#2: \frac{d}{dx} \left( \left(x - \frac{1}{4}\right)^{1/2} \cdot \left(y - \frac{1}{4}\right)^{1/2} \right)$$

$$\#3: \frac{\sqrt{4 \cdot y - 1}}{2 \cdot \sqrt{4 \cdot x - 1}}$$

$$\#4: \frac{d}{dy} \left( \left(x - \frac{1}{4}\right)^{1/2} \cdot \left(y - \frac{1}{4}\right)^{1/2} \right)$$

$$\#5: \frac{\sqrt{4 \cdot x - 1}}{2 \cdot \sqrt{4 \cdot y - 1}}$$

b) Marginal productivities at the point (3/4, 3/4):

$$\#6: \frac{1}{2}$$

$$\#7: \frac{1}{2}$$

The marginal productivities are equal. We can increase any of them.

c) Differential:  $DQ = Q'_x \cdot \text{Var}(x) + Q'_y \cdot \text{Var}(y)$

$$\#8: \frac{1}{2} \cdot \left(-\frac{1}{10}\right) + \frac{1}{2} \cdot \left(-\frac{1}{8}\right)$$

The result of that is -9/80. So, the production would decrease approximately 9/80 units.

d) Marginal rate of substitution:  $MRS = -\partial y / \partial x = -Q'_x / Q'_y$

$$\#9: -\frac{\frac{1}{2}}{\frac{1}{2}}$$

$$\#10: -1$$

If A increases 1 unit, B must decrease 1 unit to keep the production. So, if A decreases 1/4, B must increase 1/4 units.

e) Elasticity:  $E = Q'_x \cdot x / Q(x, y)$

We first calculate the present value of the production:

#11: 
$$\frac{1}{2}$$

So, the elasticity is:

#12: 
$$\frac{\frac{1}{2} \cdot \frac{3}{4}}{\frac{1}{2}}$$

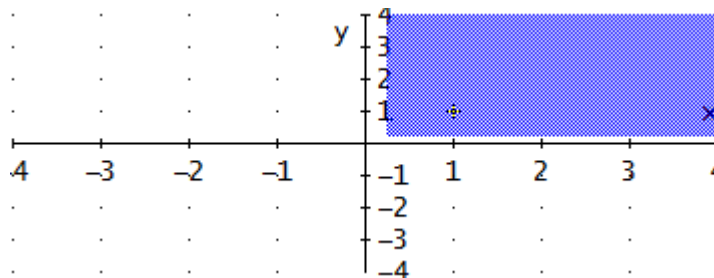
#13: 
$$\frac{3}{4}$$

The production would increase 0.75%.

f)  $Q(kx, ky) = (kx - 1/4)^{1/2} \cdot (ky - 1/4)^{1/2}$  It is imposible to write  $Q(kx, ky)$  as  $k^\alpha \cdot Q(x, y)$ .  $Q$  is not homogeneous.

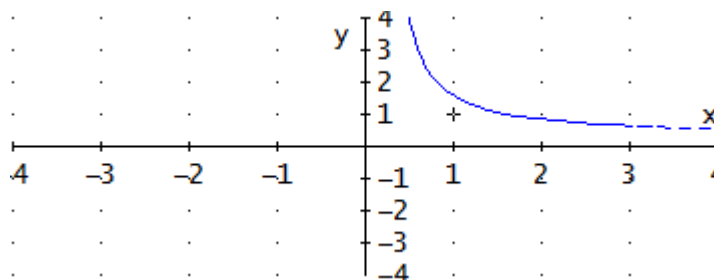
g) Dom  $Q = \{(x, y) \text{ in } \mathbb{R}^2 \text{ such that } x \geq 1/4 \text{ and } y \geq 1/4\}$

#14: 
$$x \geq \frac{1}{4} \wedge y \geq \frac{1}{4}$$



h) Isoquant of level 1.

#15: 
$$\left(x - \frac{1}{4}\right)^{1/2} \cdot \left(y - \frac{1}{4}\right)^{1/2} = 1$$



To calculate on point, I give one value to any of the variables. For

example  $x=1/2$ . I replace this value in the equation #16.

$$\#16: \left( \frac{5}{4} - \frac{1}{4} \right)^{1/2} \cdot \left( y - \frac{1}{4} \right)^{1/2} = 1$$

$$\#17: \frac{\sqrt{(4 \cdot y - 1)}}{4} = 1$$

Now I solve this equation to calculate the value of  $y$ .

$$\#18: \left( \frac{5}{4} - \frac{1}{4} \right)^{1/2} \cdot \left( y - \frac{1}{4} \right)^{1/2} = 1$$

$$\#19: \frac{\sqrt{(4 \cdot y - 1)}}{2} = 1$$

Now I solve this equation to calculate  $y$ .

$$\#20: \text{SOLVE} \left( \left[ \frac{\sqrt{(4 \cdot y - 1)}}{2} = 1 \right], [y] \right)$$

$$\#21: \left[ y = \frac{5}{4} \right]$$

The point  $(5/4, 5/4)$  is on the isoquant of level 1.